

R语言与生物统计学(2)

基础生物统计学与统计计算分析

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本节内容

- ▶ 集合操作
- ▶ 向量、矩阵、data.frame、list
- ▶ 矩阵的运算
- ▶ 读写文件
- ▶ R绘图

集合 (set) 操作：交、并、差

```
x <- 0:100
```

```
y <- seq(0, 100, by=10)
```

```
intersect(x, y); intersect(y, x) # 交:  $x \cap y$ 
```

```
union(x, y); union(y, x) # 并:  $x \cup y$ 
```

```
setdiff(x, y); setdiff(y, x) # 差:  $x \setminus y$ 
```

```
all(y %in% x); x %in% y # %in% means “belong to”
```

```
is.element(x, y); is.element(y, x)
```

```
y <- sample(y) # permutation
```

```
mymat <- match(y, x) # return the indices for each y in x  
x[mymat]
```

```
subset(x, x < 50) # 子集
```

```
which(x < 50)
```

match()函数的应用

在microarray的数据中，每个chip返回来的基因的顺序是不同的，需要把这些基因的表达数据按照相同的顺序排列起来，组成一个完整的数据集。

例如在chip1中，基因的顺序是(1,5,2,3,4)，但是在其他chip中，基因的顺序可能又不一样，这时候我们就需要match()函数，让所有的基因都按照我们预想的(1,2,3,4,5)排列

```
indices <- c(1,2,3,4,5)
```

```
mymatch <- match(indices, chip1$gene)
```

```
chip1 <- chip1[mymatch,]
```

向量

```
# vector: c(), seq(), rep()
```

```
# inner product
```

```
x <- 1:5; y <- 2:6
```

```
t(x) %*% y
```

```
sum( x * y)
```

```
# outer operation
```

```
outer(x, y, "+"); outer(x, y, "*")
```

```
# outer product
```

```
z <- x %*% t(y)
```

```
z[4, 6] == x[4] * y[6]
```

向量的内积与外积

inner product, resulting in a scalar

since vector is column vector

```
x <- 1:10; y <- 11:20
```

```
(xy.inner <- t(x) %*% y)
```

outer product, resulting in a matrix

the result is a 5by3 matrix

```
x <- 1:5; y <- 1:3
```

```
xy.outer <- x %*% t(y)
```

向量乘法的应用

```
## 计算总和、均值、方差
```

```
X <- rnorm(100)
```

```
one <- rep(1, length(X))
```

```
X.sum <- t(one) %*% X
```

```
sum(X)
```

```
X.mean <- t(one) %*% X / length(X)
```

```
mean(X)
```

```
X.var <- t(X - X.mean) %*% (X - X.mean) / (length(X) - 1)
```

```
var(X)
```

```
X - X.mean
```

```
## 向量的归一化处理
```

```
scale(X, center=T, scale=T)
```

矩阵(matrix)

数据框(data.frame)

- ▶ 矩阵的元素必须是单一的，通常为数值类型
(numeric) $\mathbb{R}^{m \times n}$
- ▶ 数据框的元素可以是多种，例如可以包含数值类型、布尔变量、分类变量等等
- ▶ 矩阵和数据框常常可以相互转化，对应的R函数分别为data.frame()和as.matrix()

矩阵

construction of a matrix, matrix() function

```
X <- matrix(1:20, nr=4, nc=5, byrow=F)
```

```
x <- 1:5
```

```
y <- 5:1
```

```
A <- cbind(x, y) # column binding
```

```
B <- rbind(x, y) # row binding
```

an element of a matrix

```
X[4,3]
```

subset of a matrix

```
X[1:3,] # return the rows 1-3
```

```
X[-4, c(3,2,4,5)] # return the columns 3, 2, 4, 5 except the 4th row
```

```
X[, sample(1:5)] #permute the columns
```

矩阵的运算

```
x <- matrix(1:25, 5, 5)
```

```
y <- matrix(1:25, 5, 5)
```

```
x + y; x - y
```

```
yt <- t(y) # transposition
```

```
x * y # element-wise multiplication
```

```
z <- x %*% y # matrix multiplication
```

```
z
```

```
z[3,5] == sum(x[3,] * y[,5])
```

```
all(z[,5] == x %*% y[,5])
```

矩阵的乘法

- ▶ ## 矩阵A、B相乘，满足的条件是A的列数必须与B的行数相等
- ▶ ## $C=AB$ ，则C的 $c[i,j] = \text{sum}(a[i,]*b[,j])$
- ▶ ## 也就是说 $c[i,j]$ 是向量 $a[i,]$ 与 $b[,j]$ 的点积
- ▶ `A <- matrix(1:16, 4, 4)`
- ▶ `B <- matrix(1:20, 4, 5)`
- ▶ `C <- A %*% B`
- ▶ `M <- matrix(NA, 4, 5)`
- ▶ `for (i in 1:4) for (j in 1:5) M[i,j] <- sum(A[i,]*B[,j])`
- ▶ `all(M==C)`

- ▶ ## 另一种看法则是 $c[,j]$ 是A的列向量 $a[,k]$ 的线性组合
- ▶ ## 其权重系数为 $b[k,j]$, $c[,j]=\text{sum}(a[,k]*b[k,j])$
- ▶ `X <- matrix(0, 4, 5)`
- ▶ `for (k in 1:5) for (m in 1:4) X[,k] <- X[,k] + A[,m]*B[m,k]`
- ▶ `all(X==C)`

- ▶ ## 此外，矩阵C还可以看作r个矩阵 $C[k]$ 的和，其中每个矩阵 $C[k]$
- ▶ ## 都是A的列向量和B的行向量的外积
- ▶ `D <- list()`
- ▶ `for (r in 1:4) D[[r]] <- outer(A[,r], B[r,])`
- ▶ `E <- matrix(0,4,5)`
- ▶ `for (k in 1:4) E <- E + D[[k]]`
- ▶ `all(E==C)`

矩阵乘法的应用

```
x <- matrix(1:20, 4, 5)
rowMeans(x)
apply(x, 1, mean)
colMeans(x)
apply(x, 2, mean)
one1 <- rep(1, dim(x)[1])
x.means <- t(one1) %*% x / dim(x)[1]
one2 <- rep(1, dim(x)[2])
as.vector(x %*% one2 / dim(x)[2])
x.diff <- x - one1 %*% x.means
(x.scaled <- scale(x, center=T, scale=F))
x.cov <- t(x.diff) %*% x.diff / (dim(x)[1]-1)
cov(x)
```

list

list常常作为函数的返回结果，尤其是当返回结果不只一个的时候

```
## list
```

```
xl <- list()
```

```
xl[[1]] <- c(1,3,5)
```

```
xl[[2]] <- "standard normal distribution"
```

```
xl[[1]][2]
```

```
x
```

```
f <- function(x) {
```

```
  mean <- mean(x);
```

```
  sd <- sd(x);
```

```
  return(list(m=mean, s=sd))
```

```
}
```

```
x <- rnorm(100)
```

```
xf <- f(x)
```

```
xf
```

```
xf$m; xf$s
```

控制结构

```
## if (...) { dosomething(); }  
## else { doanotherthing(); }  
## another kind of structure  
c <- rnorm(100)  
x <- ifelse(c >= 0, 1, -1)  
## while (condition) { dosomething }  
for (i in 1:10) cat(i);
```

函数型语言

函数的定义

```
f <- function(x) {  
  return(x^2+2*x+1)  
}
```

调用函数

```
x <- rnorm(1000)  
y <- f(x)  
plot(x, y, type="l")  
cor(x, y) ## correlation coefficient
```

apply(), sapply(), lapply()

apply() used for one dimension of an array or data.frame

```
x <- matrix(1:20, 4, 5)
```

```
apply(x, 2, median)
```

```
apply(x, 1, sum)
```

lapply() return a list

```
M <- list(m=3, n=c(TRUE, FALSE, TRUE), r=4:7)
```

```
lapply(M, quantile)
```

sapply() used for each element of a vector

the return result is a vector

```
x <- sapply(1:5, seq)
```

```
lapply(x, fivenum)
```


tapply与aggregate

```
## tapply() will return a table  
data(warpbreaks)  
warpbreaks  
tapply(warpbreaks$breaks, warpbreaks[,-1], sum)  
aggregate(warpbreaks[,1], by=c(warpbreaks[,-1]), sum)
```

```
## it can be treated as the weighed version of table()  
## 比如我们在工作中，需要考察(吸烟, 肺癌)和血压的关系  
## 我们会用tapply()统计(+,+), (+,-), (-,+), (-,-)的平均血压  
## 而table()只能统计这四组的人数
```

因子水平factor

```
### 产生因子水平
## gl(n,p,length)
# n          -          因子水平数
# p          -          同一水平重复试验次数
# length     -          总样本大小
gender <- rep(c('male','female'), each=8)
gender <- factor(gender)
## 直接用gl函数就要简单的多了
(gender <- gl(2,8,labels=c('male','female')))
(gender2 <- gl(2,1,length=16, labels=c('male','female')) # balanced
(gender3 <- gl(2,2,length=16, labels=c('male','female')) # balanced
(gender4 <- gl(2,3,length=16, labels=c('male','female')) # imbalanced
table(gender)
table(gender2)
table(gender3)
table(gender4)
```

变量的初始化

```
x <- numeric()
xl <- list()
M <- matrix(NA,3, 4)
D <- data.frame(M)
rownames(D) <- paste("R", 1:3, sep="")
colnames(D) <- paste("C", 1:4, sep="")
class(x)
class(str)
typeof(x)
typeof(string)
mode(x)
mode(string)
```

读写文件

- ▶ `scan()`函数可以读取单个向量
- ▶ `read.table()`函数可以读取以TAB作为分隔符的表，读入的结果为一个`data.frame`
- ▶ `read.csv()`可以读取以comma为分割符的表
- ▶ `read.delim()`等可以读取任意分隔符的表

- ▶ 写文件用`write.table()`函数将变量保存为文本文件；
- ▶ 还可以用`save.image()`和`save()`函数将变量存取为二进制文件`*.RData`
- ▶ `*.RData`文件可以用`load()`命令载入

scan()

```
x <- scan("number.txt")
```

```
x
```

```
0.312  
0.46  
0.374  
0.411  
0.974  
0.645  
0.392
```

read.table()

```
x <- read.table("scores.txt", header=T,  
  row.names=1)
```

```
x$math
```

```
names(x)
```

```
class(x)
```

```
attach(x)
```

```
math
```

```
x
```

	math	english	physics
Peter	95	79	89
John	45	99	58
Elaine	78	60	88

用read.table()读取birthweights.dat

Variable	Abbreviation
Birth Weight in Grammes	BWT
Low Birth Weight (0 = BWT \geq 2500g, 1 = BWT < 2500g)	LOW
Age of Mother in Years	AGE (A)
Weight in Pounds at Last Menstrual Period	LWT
Race (1 = White, 2 = Black, 3 = Other)	RACE (R)
Smoking Status during Pregnancy (0 = No, 1 = Yes)	SMOKE (S)
History of Premature Labor (0 = None, 1 = One, etc.)	PTL (P)
History of Hypertension (0 = No, 1 = Yes)	HT (H)
Presence of Uterine Irritability (0 = No, 1 = Yes)	UI (U)
Number of Physician Visits in First Trimester (0 = None, 1 = One, etc.)	FTV (F)

部分R code

```
bwt <- read.table("birthweights.dat",  
                 header=T)
```

```
## 基本统计
```

```
summary(bwt)
```

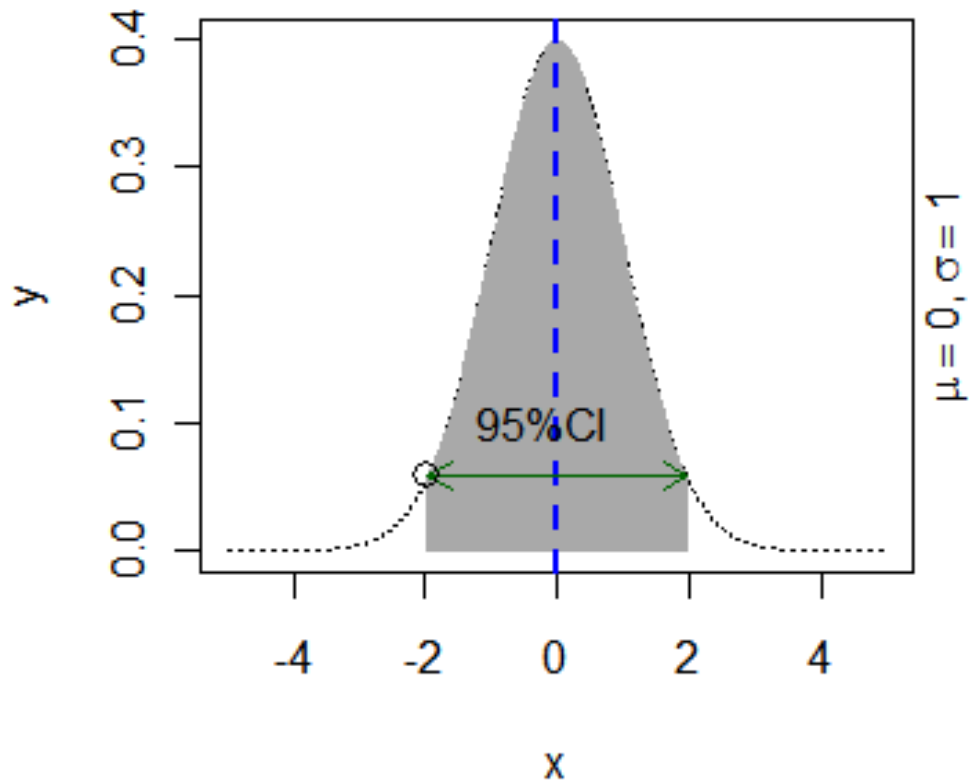
```
str(bwt)
```

```
bwt$BWT
```

```
attach(bwt)
```

```
BWT
```


$X \sim N(0, 1)$



R绘图

基本绘图函数

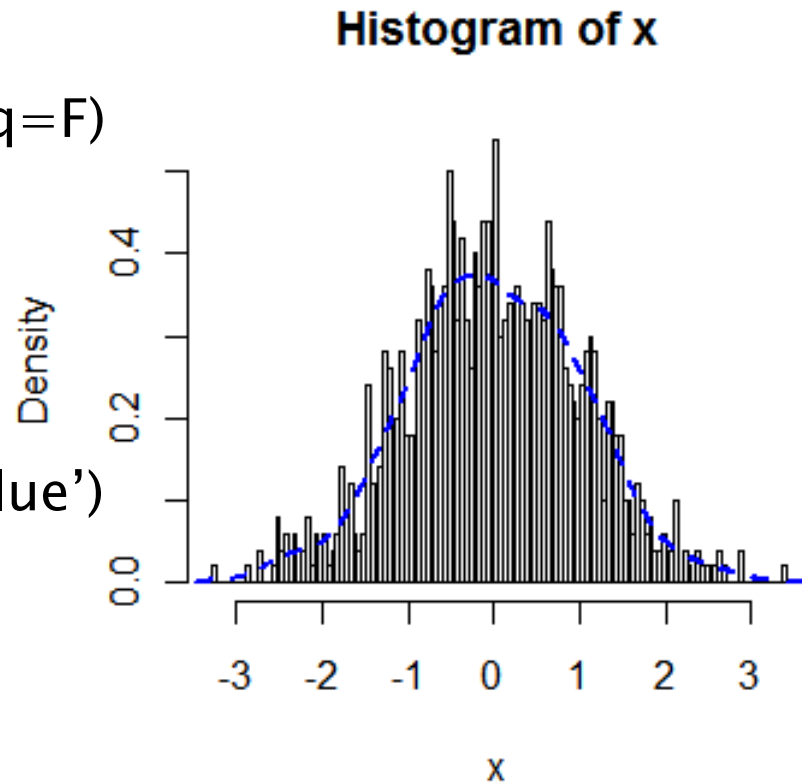
- ▶ 常用的绘图函数主要有
 - hist(): 直方图, 显示分布频率或密度
 - barplot(): 条形图, 常用于多个样本分类频率的比较
 - boxplot(): 盒状图, 常用于多个组分布的比较
 - plot(): 基本画图函数, 散点图或者折线图等
 - points(): 基本绘图函数, 画散点, 不能单独使用
 - lines(): 折线图, 不能单独使用
 - segments(): 绘制线段, 不能单独使用
 - arrows(): 绘制箭头, 箭头的形状大小要注意设置
 - rect(): 绘制四边形的函数
 - polygon(): 绘制多边形的函数
 - abline(): 绘制直线
 - axis(): 绘制坐标
 - box(): 为图形添加外框

绘图函数（续）

- `text()`: 在指定坐标添加文字
- `mtext()`: 在坐标变上添加文字说明
- `legend()`: 添加图示说明
- `identify()`: 为数据点添加标注
- ▶ 比较复杂的绘图函数
 - `contour()`: 类似等高线图
 - `persp()`: 立体的侧面视图
 - `image()`:
 - `curve()`: 可以用来绘制指定方程的曲线

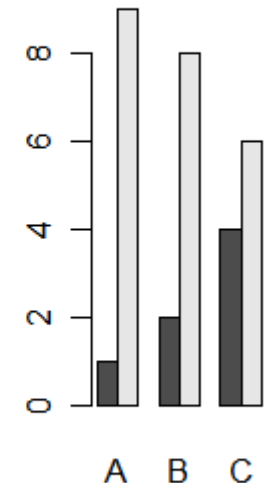
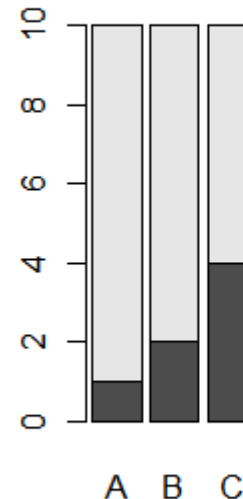
histogram

```
x <- rnorm(1000)
hx <- hist(x, nclass=120, freq=F)
names(hx)
hx$breaks
hx$mids
hx$counts
lines(density(x), lty=2, col='blue')
```



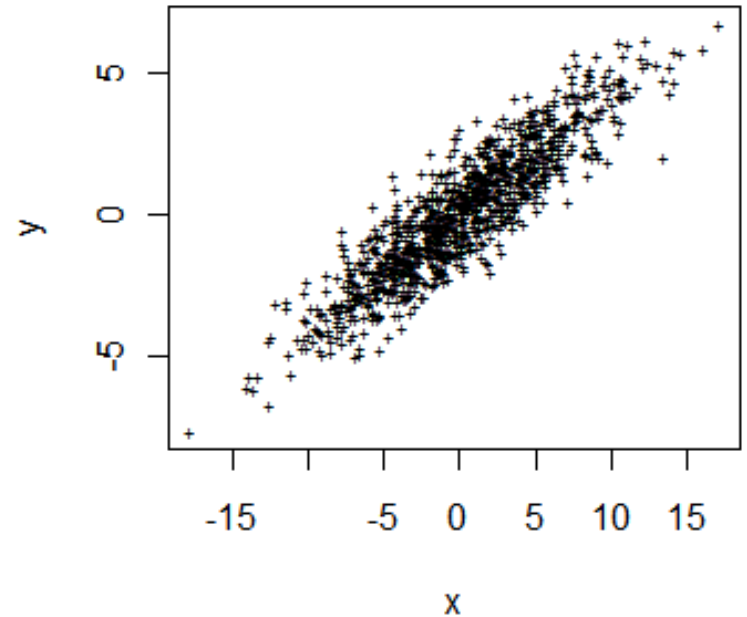
barplot

```
x <- matrix(c(1,9,2,8,4,6), 2, 3)
colnames(x) <- LETTERS[1:3]
par(mfrow=c(1,2))
barplot(x, beside=T,
        col=c("red", "blue"))
barplot(x, beside=F)
```



scatterplot

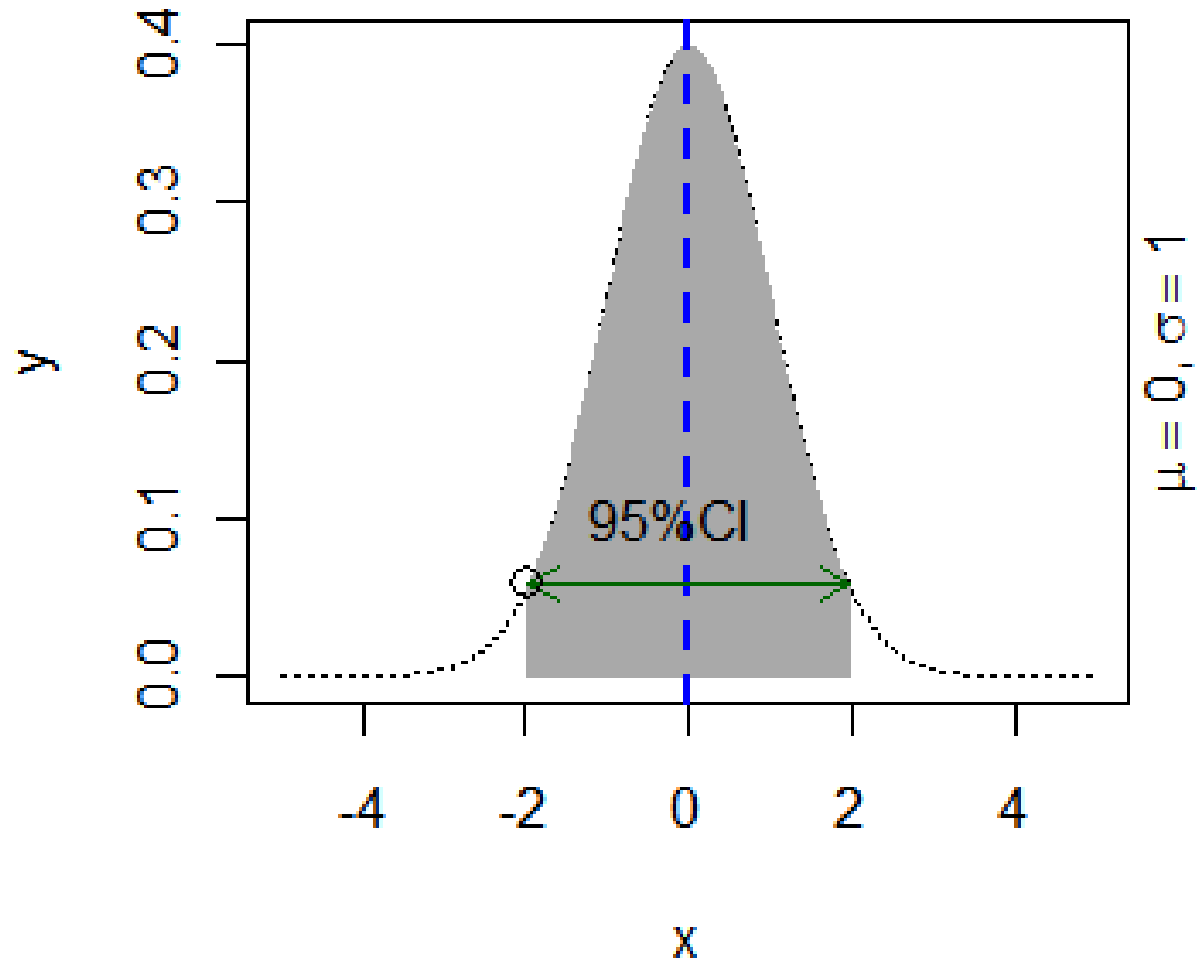
```
x <- 5*rnorm(1000)
y <- 0.4 * x + rnorm(1000)
plot(x, y, pch="+", cex=.6)
abline(c(0, .4))
```



组合图：线段、箭头、图标

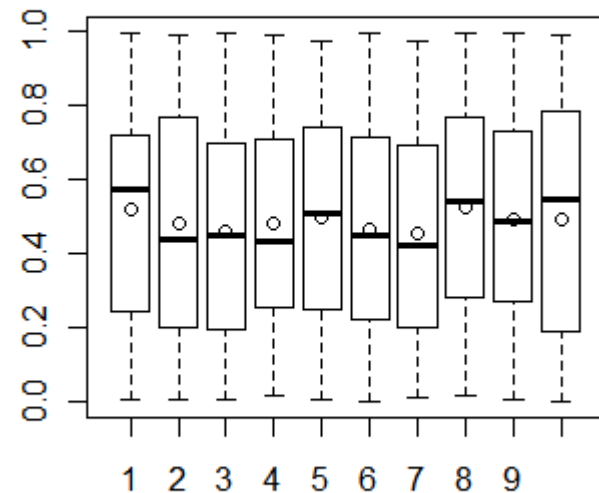
```
x <- seq(-5, 5, length=1001)
y <- dnorm(x)
plot(x, y, type='n')
lines(x,y,lty=3)
x0 <- qnorm(0.025)
x1 <- qnorm(0.975)
segments(x0,0,x0,dnorm(x0))
segments(x1,0,x1,dnorm(x1))
curve(dnorm, x0, x1, add=T, type="h", col='darkgray')
abline(v=0, lty=2, lwd=2, col='blue')
text(-.20, .1, "95%CI")
arrows(x0, dnorm(x0), x1, dnorm(x1), length=.1, code=3,
       col='darkgreen')
symbols(x0, dnorm(x0), circles=0.2, add=T, inches=F)
mtext(expression(paste(mu==0, ", ", sigma==1)), 4)
title(expression(paste(X,"~", N(0,1))))
```

$$X \sim N(0, 1)$$



boxplot

```
x <- matrix(rnorm(1000), 100, 10)
boxplot(x)
x <- matrix(runif(1000), 100, 10)
xbox <- boxplot(x)
names(xbox)
xmean <- apply(x, 2, mean)
xmed <- apply(x, 2, median)
library(e1071)
xskew <- apply(x, 2, skewness)
xskew > 0; xmean > xmed
points(1:10, xmean)
```



辅助图

axis()

text()

mtext()

legend()

R simulation

```
xmeans <- NULL
for (i in 1:1000) {
  x <- rnorm(100, 0, 4)
  xmeans <- c(xmeans, mean(x))
}
xmeans
mean(xmeans)
var(xmeans)
sd(xmeans)
## 从结果你看到了什么结论？
```